

# Reaction Experiments with Exotic Beams

Antti Saastamoinen

Cyclotron Institute  
Texas A&M University

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# Why Nuclear Reactions?

Nuclear reactions in general are used to:

1. Produce other nuclei:

*samples, sources, **new elements, isotopes for applications, (radioactive ion / rare isotope / exotic) beams***

*choose your favorite expression*

2. Study some properties of a nucleus of choice  
in a **reaction experiment** for:

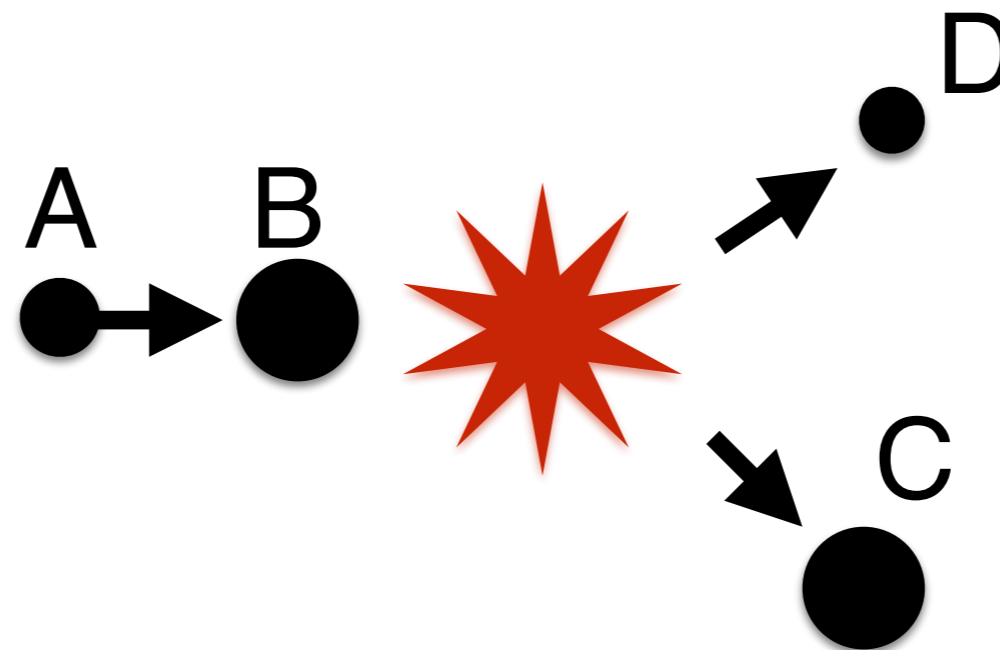
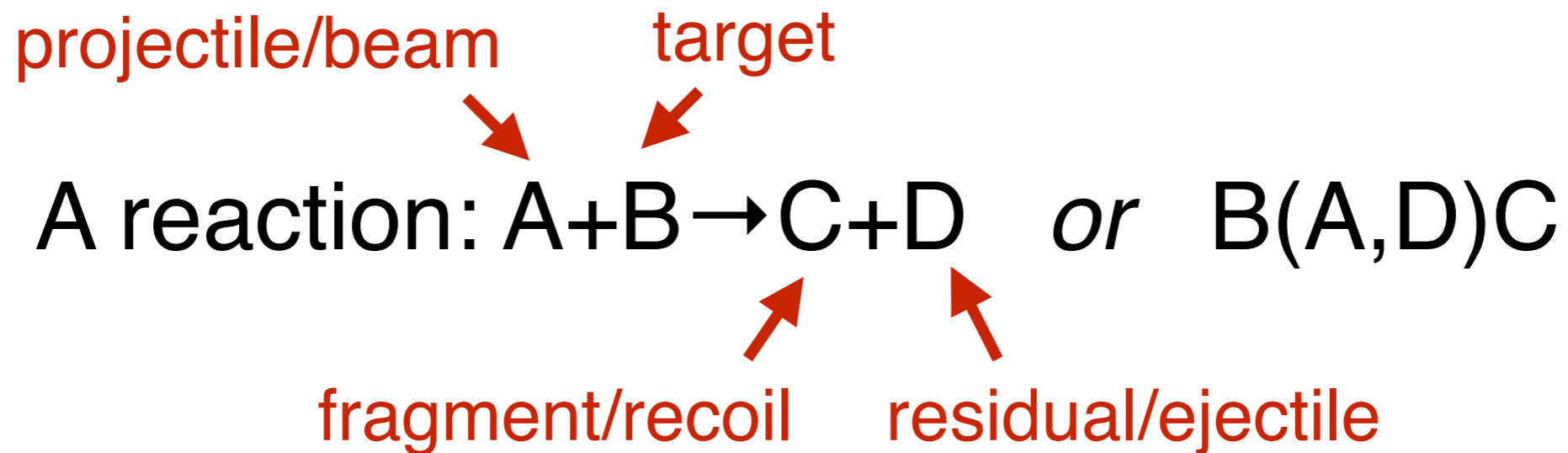
*nuclear structure, astrophysics, reaction mechanisms, stockpile stewardship,...*

3. Study nuclear dynamics and nuclear matter  
equation of state

# Outline of these lectures

- few basics of reaction experiments
- different reaction types
- production of exotic beams for reaction experiments
- some experimental considerations
- examples reaction experiments with exotic beams

# Some basic notations



Normal kinematics:  $a+B \rightarrow C+d$ ;  $B(a,d)C$ ,  $M_{\text{projectile}} < M_{\text{target}}$   
Inverse kinematics:  $B+a \rightarrow d+C$ ;  $a(B,C)d$ ,  $M_{\text{projectile}} > M_{\text{target}}$



# Conservation laws

Things that are considered conserved in nuclear reactions:

Energy

Linear momentum

Proton and neutron (baryon) number

Charge

Angular momentum

Parity

Isospin

# Reaction Q-value

Reaction Q- value: amount of energy released in the reaction

$$Q = \sum_i ME_i - \left( \sum_f ME_f + E_f^* \right) = (M_{beam} + M_{target})c^2 - \sum_{products} (M_{product}c^2 + E_{excitation,product})$$

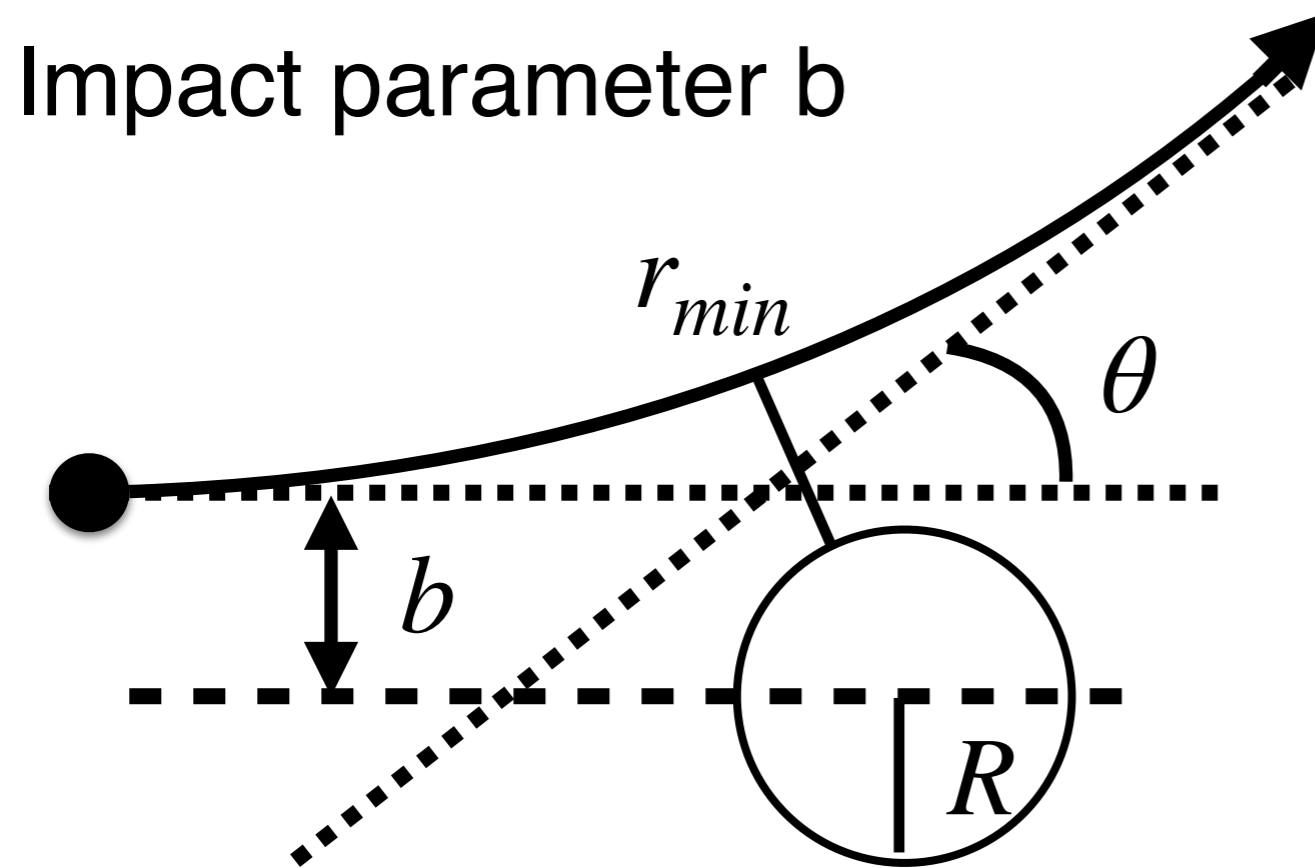
Most convenient to use mass excesses (ME) or binding energies (BE).  
Evaluated values available e.g. through <https://www-nds.iaea.org/amdc/>  
(various vintages of these evaluations are found through out codes, be careful if working on something very recent and code uses something older!)

$Q < 0$ : endothermic reaction, requires energy input to make it work

$Q > 0$ : exothermic reaction, energy is released, can occur if otherwise possible

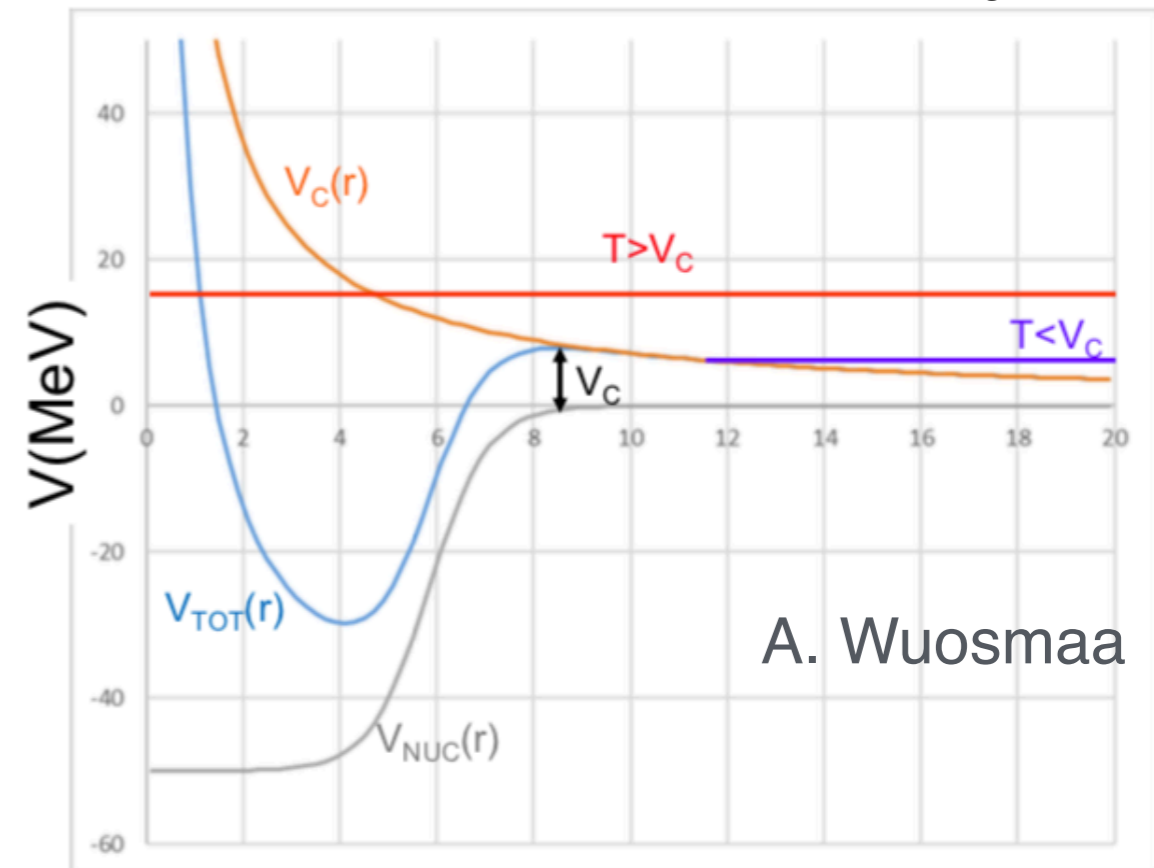
Important to consider when choosing what reaction to use!  
(reaction energy threshold, momentum matching,  
which states to populate, kinematics...)

# Few important parameters for reactions



## Coulomb barrier height

$$V_c(\text{MeV}) \approx 1.44 \frac{Z_{beam} Z_{target}}{1.2(A_{beam}^{1/3} + A_{target}^{1/3})}$$



## Classical deflection equation:

$$\theta(b) = \pi - 2b \int_{r_{min}}^{\infty} \frac{dr}{r^2 \sqrt{1 - (b/r)^2 - V_{tot}(r)/E}}$$

←  $V_{tot}(r) = V_c(r) + V_{nuc}(r), E = mv^2/2$

$$L = \vec{r} \times \vec{p} = rpsin\phi = bp$$

L conserved for fixed b

$$\Delta L = qb = (p_f - p_i)b \approx qR \text{ on surface}$$

For experiment we can only choose:  
Target, Beam, Energy, and Polarization

# Types of Nuclear Reactions

- Elastic scattering:  $A+B \rightarrow A+B$   
(no energy exchange)
- Inelastic scattering:  $A+B \rightarrow A+B^*$   
(energy exchange, no mass or charge exchange)
- Transfer of one or more nucleons  $x$ :  $(A=C+x)+B \rightarrow C+(D=B+x)$   
(mass and/or charge exchange)
- Breakup/knockout:  $A+B \rightarrow B+C+D$   
(projectile breaks due to interaction with the target)
- Compound nuclear reaction:  $A+B \rightarrow C^* \rightarrow D+E$   
(formation of a short lived intermediate nucleus)
- Radiative capture:  $A+B \rightarrow C+\gamma$   
(projectile captured by target, de-excitation via photon)
- Photo-disintegration:  $C+\gamma \rightarrow A+B$   
(inverse of radiative capture)
- Fission:  $A + B \rightarrow C+D+ x \text{ neutrons}$   
(A typically neutron; B e.g. U, Pu; C,D heavy fragments)

# Nuclear Reaction Timescale

Higher impact parameter

Peripheral

Central

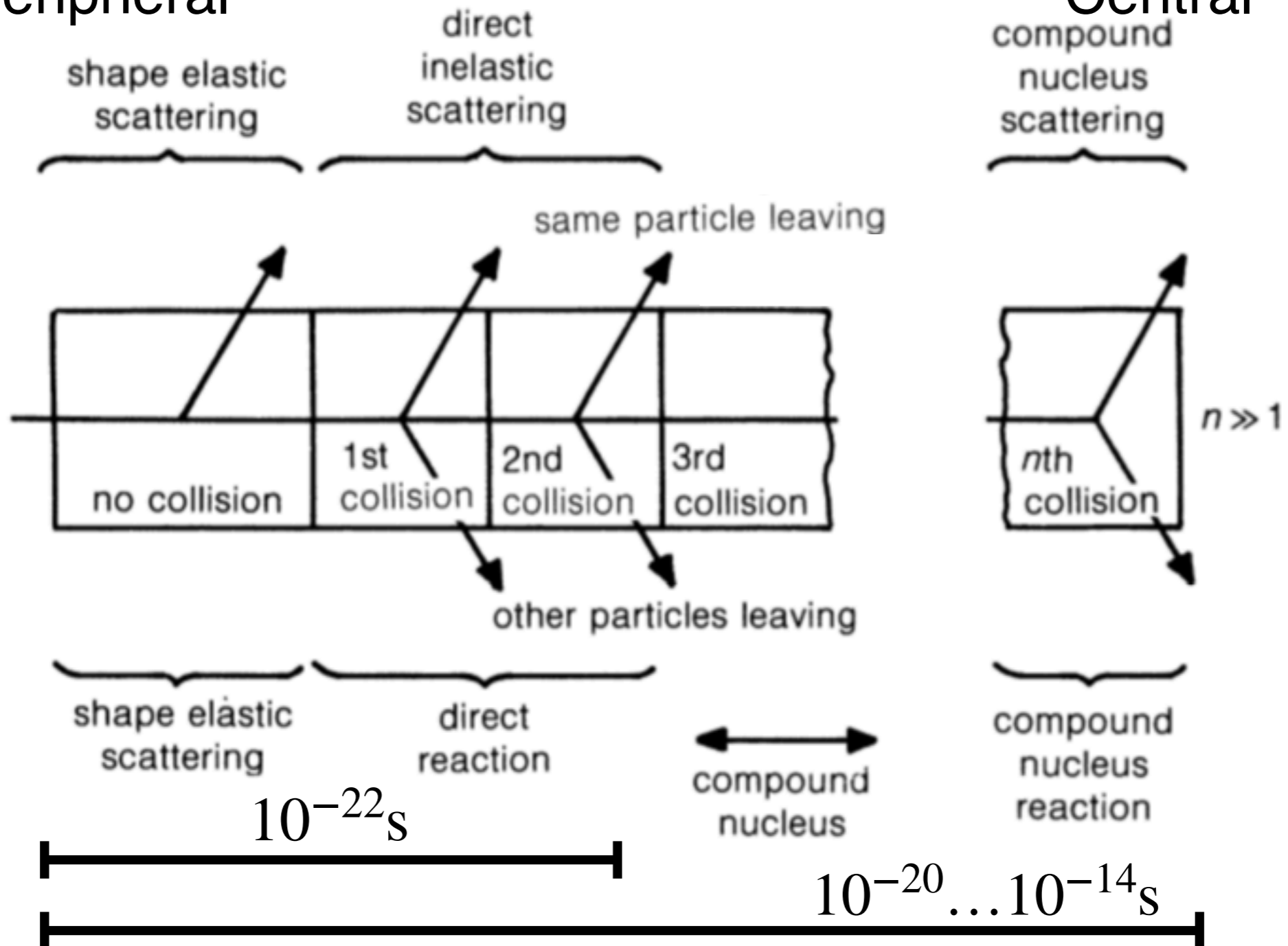
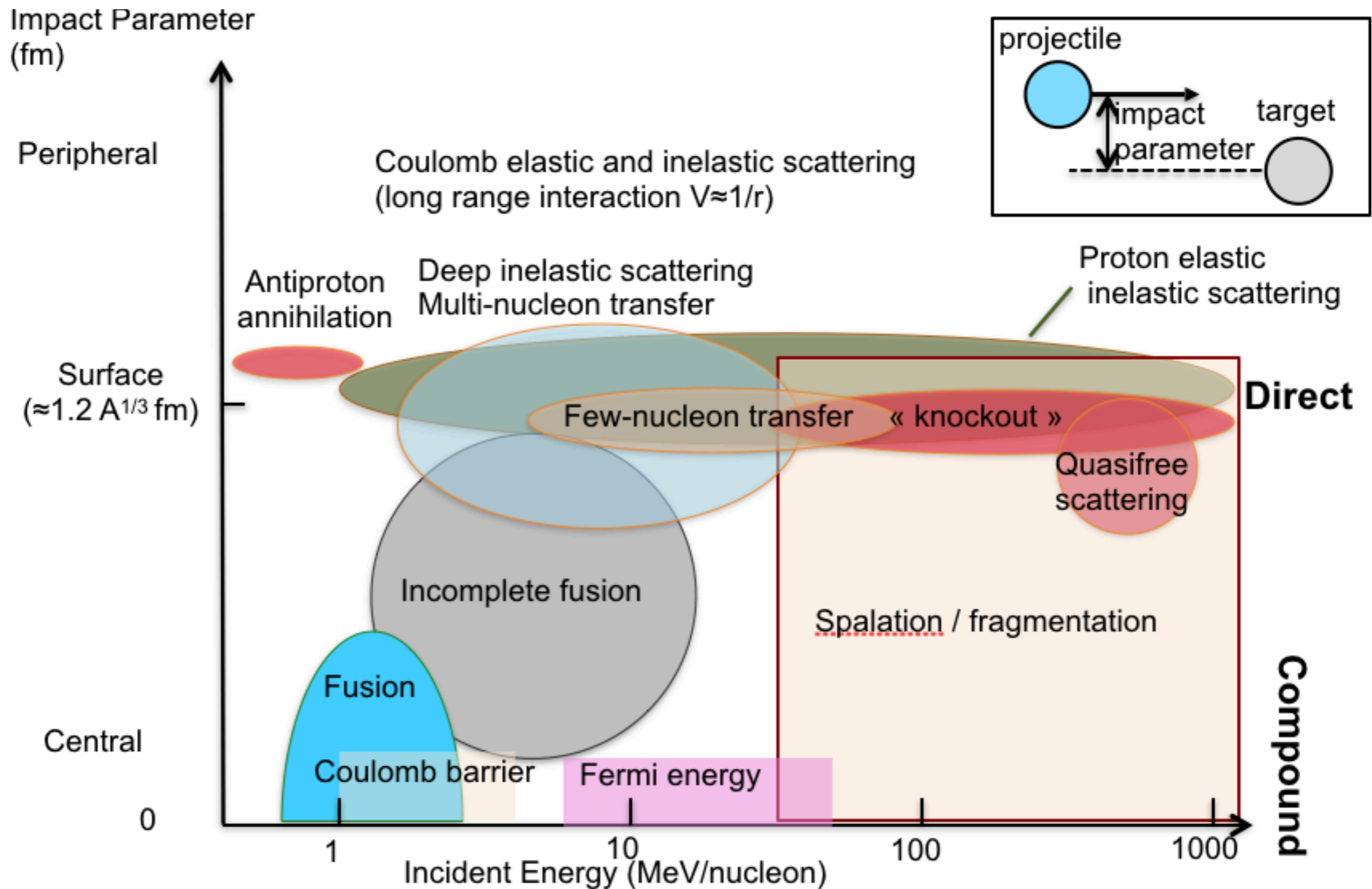


Image credit: R.J. Blin-Stoyle, Nuclear and particle physics

# Reaction Types: Impact Parameter vs Energy



A. Obertelli / Euroschool on Exotic Beams 2016

# What do we measure in a reaction experiment?

Our instruments measure **Energy** and **Time** of the beam components, reaction products,  $\gamma$ /X-rays, ...  
→ *Particle identification (PID) of beam/products ( $dE/dx$ , ToF, ...),  
Energy levels of the states involved, ...*

We know the **positions and coverage** of our instruments relative to the beam and the target  
→ *Kinematics, angular distributions, ...*

We **count** the amount of these interactions with known **efficiencies**  
→ *Probabilities of the reactions, cross sections, branching ratios, ...*

One can **polarize** the beam or the target  
→ *Spin orientation, spin dependence of reaction cross section*

See Tony Ahn's lectures for the techniques how



# Cross sections

Most reaction experiments measure a cross section in some form (probability of a reaction taking place) e.g. some of these

$$\sigma \quad \sigma(\theta) \quad \sigma(E)$$

*Integrated cross sections*

$$\frac{d\sigma}{d\Omega} \quad \frac{d\sigma}{dE} \quad \frac{d^2\sigma}{dEd\Omega}$$

*Differential cross sections*

Shape and angular distribution of cross section:


- information about reaction mechanism (theory!)
- properties of residual nuclei: size, shape, spins and parities of levels,...

Energy dependence:

- information about reaction mechanism (theory!)
- identify resonances

Unit is “barn”: 1 barn =  $10^{-24}$  cm<sup>2</sup>, millibarn =  $10^{-27}$  cm<sup>2</sup> very common

*“Just for fun, some have referred to the microbarn as an outhouse, but you’ll probably never find that in a peer-reviewed publication.”*

*S. Goldfarb & K. Anthony, Nature Physics 15, 414 (2019).* Who can get  into LaTeX?!



# Differential cross section: Experiment meets Theory

This we can measure  
at given angle and incident energy


$$\left(\frac{d\sigma}{d\Omega}\right)_{exp} = C^2 S \left(\frac{d\sigma}{d\Omega}\right)_{theory}$$

This has the nuclear structure:

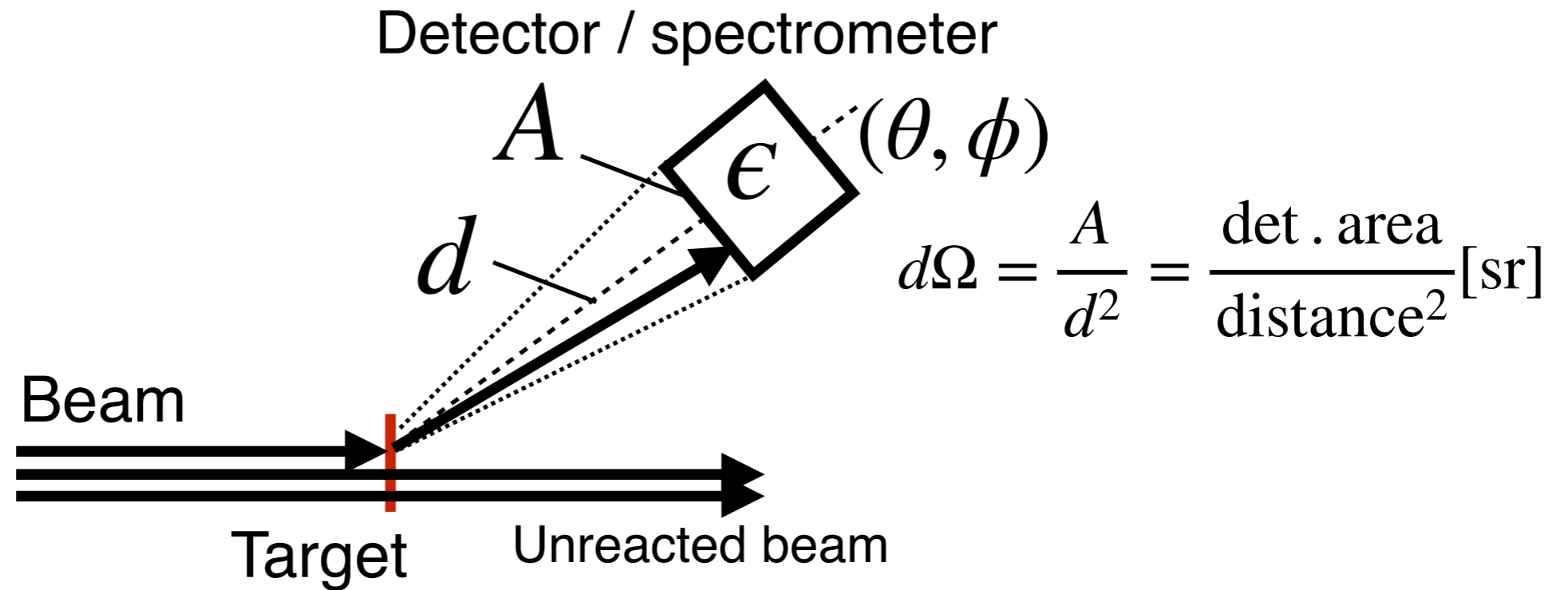
This has the reaction model  
from your favorite /most applicable  
theoretical description

$C^2$ : a statistical factor (Glebsch-Gordan coef.),  
omitted in some texts

$S$ : spectroscopic factor

Most common unit: mbarn/sr =  $10^{-27}$  cm<sup>2</sup>/sr     /sr?

# How to measure: Differential cross section



$$\left( \frac{d\sigma}{d\Omega} \right)_{exp} = \frac{N_{Detected}(\theta, \phi)}{N_{Beam} \cdot N_{Target} \cdot \epsilon \cdot d\Omega}$$

Integrated counts from detector / spectrometer

Integrated beam particles

Non-overlapping target atoms in target per unit area [ $1/\text{cm}^2$ ]  
(careful with composite targets!)

Detector / spectrometer efficiency [unitless] & solid angle / acceptance [sr]

# About exotic beam reaction kinematics

Traditionally reaction experiments done with light projectile on heavier stable target — “*normal kinematics*”

Most of the exotic beam reaction experiments done with a projectile on typically much lighter target — “*inverse kinematics*”

→ Energy - angle systematics are quite different and need to be careful in coordinate transformations between the laboratory and center of mass frames

$$\left(\frac{d\sigma}{d\Omega}\right)_{lab} = \frac{1 + \gamma^2 + 2\gamma\cos\theta_{cms}}{|1 + \gamma\cos\theta_{cms}|} \cdot \left(\frac{d\sigma}{d\Omega}\right)_{cms}, \quad \gamma = v_{cms}/v_{ejectile}$$

Good reads on topic, e.g. :

W. Catford, LNP879, 67 (2014),

J.S. Winfield et al., NIM A 396, 147 (1997)

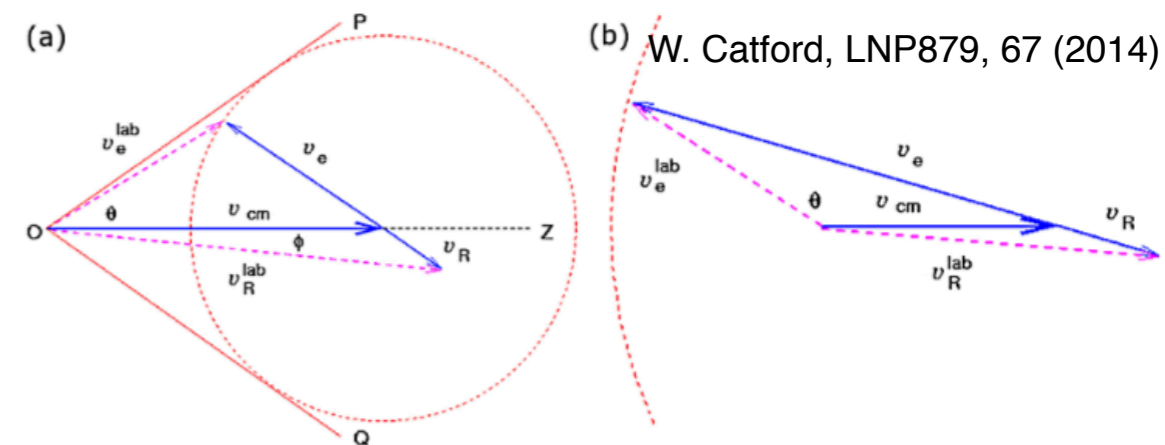


Fig. 3.10 Velocity addition diagrams (a) for a typical pickup reaction such as (p, d) or (d, t), and (b) for a typical stripping reaction such as (d, p). Certain assumptions about the beam energy and the reaction Q-value are described in the text

# Reaction Kinematics: Useful Tools for Experimentalist

- LISE++ program by O. Tarasov et al.  
(includes a relativistic kinematics calculator)  
<http://lise.nscl.msu.edu/lise.html>  
O.Tarasov, D.Bazin, NIM B 266, 4657 (2008).  
D.Bazin, O.Tarasov, M.Lewitowicz, O.Sorlin, NIM A 482 307 (2002).
- CATKIN by W. Catford  
(Relativistic 2 body kinematics in Excel):  
<http://personal.ph.surrey.ac.uk/~phs1wc/kinematics/>
- Two-Body Kinematics Calculator and Plotter by S. Sjue:  
<http://skisickness.com/2010/04/relativistic-kinematics-calculator/>
- NPTOOL by A. Matta et al. (GEANT4/ROOT simulation / analysis framework, has e.g. kinematics plotting in ROOT command line)  
<http://nptool.org/>  
A. Matta et al., J. Phys. G 43, 045113 (2016).

# Example: $E_3$ vs $\theta_{3cm}$ line for $d(^{28}\text{Si}, p)^{29}\text{Si}$ @ 10 MeV/u

## Two-Body Kinematics Calculator and Plotter

This script generates plots and tables representing products of nuclear reactions, along with elastic and inelastic scattering processes using relativistic kinematics. Enter the particles or nuclei involved, the kinetic energy of the projectile, any excitation energy of the products and select the desired output. The plots and tables created will be shown at the bottom of the page.

Enter Isotopes ( $^A\text{E}$ ) or Masses (AMU or MeV). Isotopes should be of form 1H, 4He,  $^{16}\text{O}$  ... etc, case insensitive; n, p, d, t, h, a, g, e (or e-) and e+ are also accepted as shorthand for neutron, proton, deuteron, triton,  $^3\text{He}$ , alpha, gamma, electron and positron. Shorthand is also available for particles via pi+, pi-, pi0, rho+, rho-, rho0, k+, k-, k0, mu, mu+, mu-, tau, tau+ and tau-. More could be added by request. Isotope masses are taken from the table of atomic masses, [mass.mas114](#), with  $Zm_e$  subtracted.

Please note: the notation has been changed so that  $m_1$  has the kinetic energy. For an explanation of the calculations, see [Relativistic Reaction Kinematics](#)

Projectile ( $m_1$ ): 28Si   $^A\text{E}$   AMU  MeV  $\rightarrow m_1 = 26053.18600326$  MeV  
 Target ( $m_2$ ): d   $^A\text{E}$   AMU  MeV  $\rightarrow m_2 = 1875.61277883$  MeV  
 Ejectile ( $m_3$ ): p   $^A\text{E}$   AMU  MeV  $\rightarrow m_3 = 938.27199964$  MeV  
 Recoil ( $m_4$ ): 29Si   $^A\text{E}$   AMU  MeV  $\rightarrow m_4 = 26984.27774703$  MeV

Projectile Energy: 280 MeV  kinetic  total  
 Ejectile Excitation Energy: MeV  
 Recoil Excitation Energy: MeV

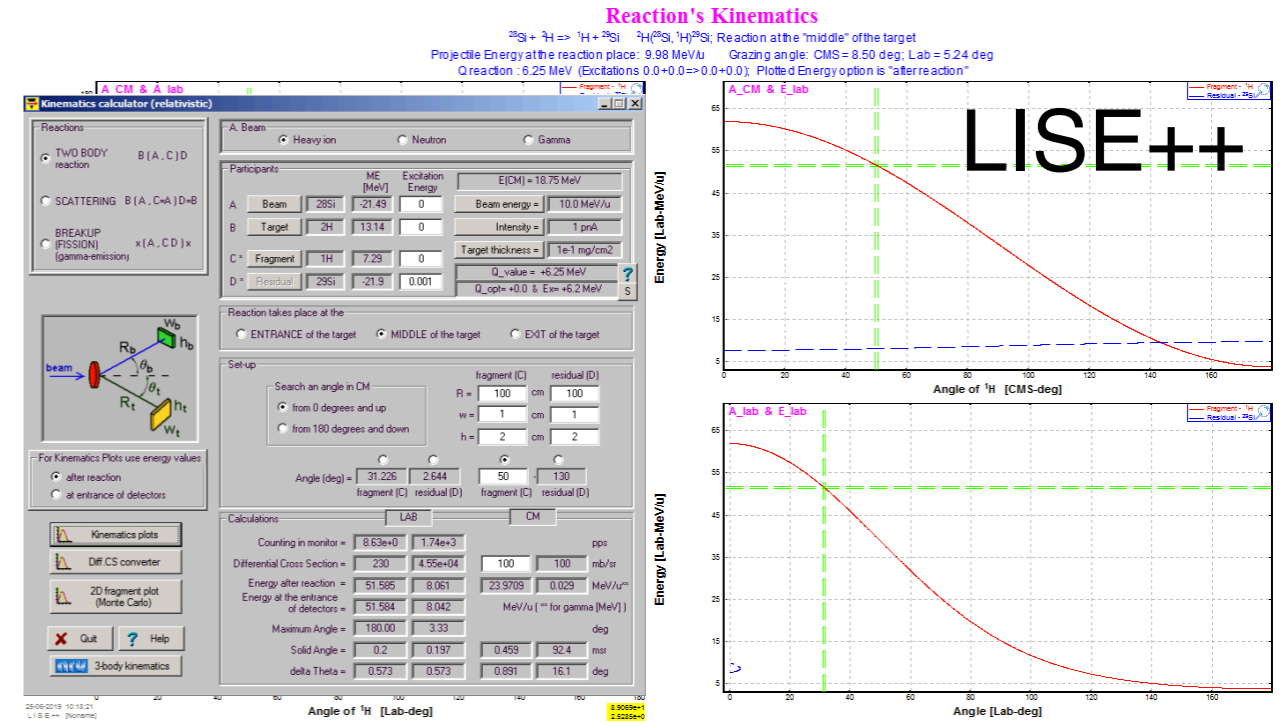
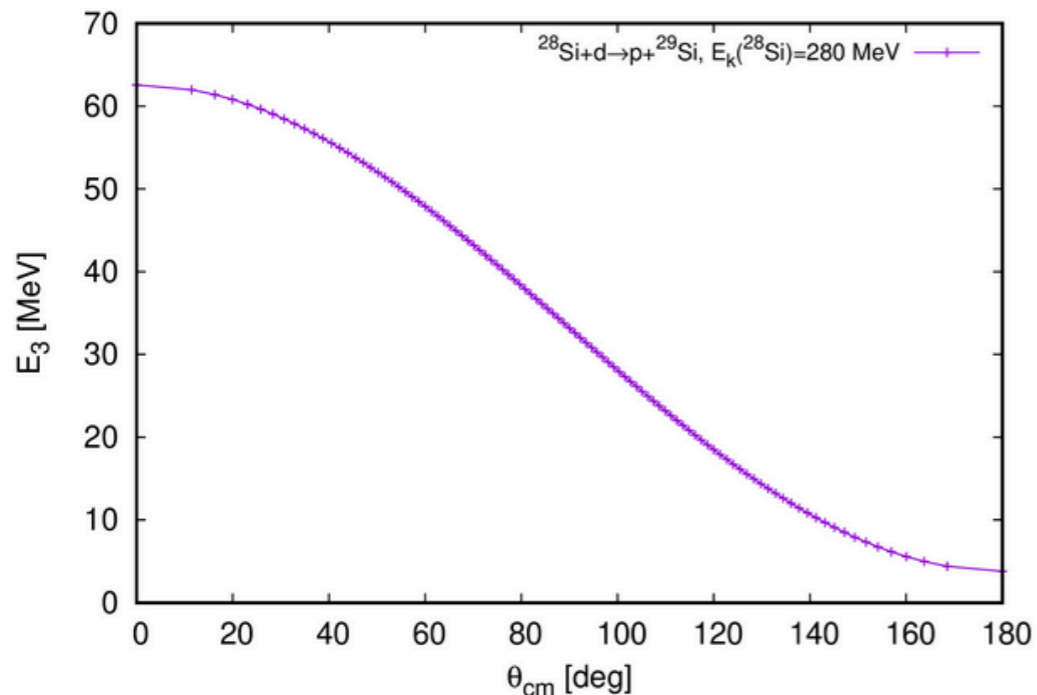
Plot Abscissa (x-axis):   $\theta_3$    $\theta_4$    $\theta_{3cm}$    $\cos(\theta_{3cm})$    $E_3$    $E_4$    $v_3$    $v_4$    $d\Omega_3/d\Omega_{cm}$    $d\Omega_4/d\Omega_{cm}$   
 Plot Ordinate (y-axis):   $\theta_3$    $\theta_4$    $\theta_{3cm}$    $\cos(\theta_{3cm})$    $E_3$    $E_4$    $v_3$    $v_4$    $d\Omega_3/d\Omega_{cm}$    $d\Omega_4/d\Omega_{cm}$   
 Express angles in:  degrees  radians  
 x min, x max:    
 y min, y max:    
 Plot Width: 900 pixels, Font Size: 21 pt  
 Number of Points: 100  
 Legend Font Size: 16 pt, Legend Vertical Displacement: 3 %  
 Output:  display PNG image  generate EPS file  generate PDF file  
 Include:   $^{28}\text{Si}+d \rightarrow p+^{29}\text{Si}$ ,  $E_k(^{28}\text{Si})=280$  MeV (check channels to keep them)

## Two-Body Kinematics (webpage)

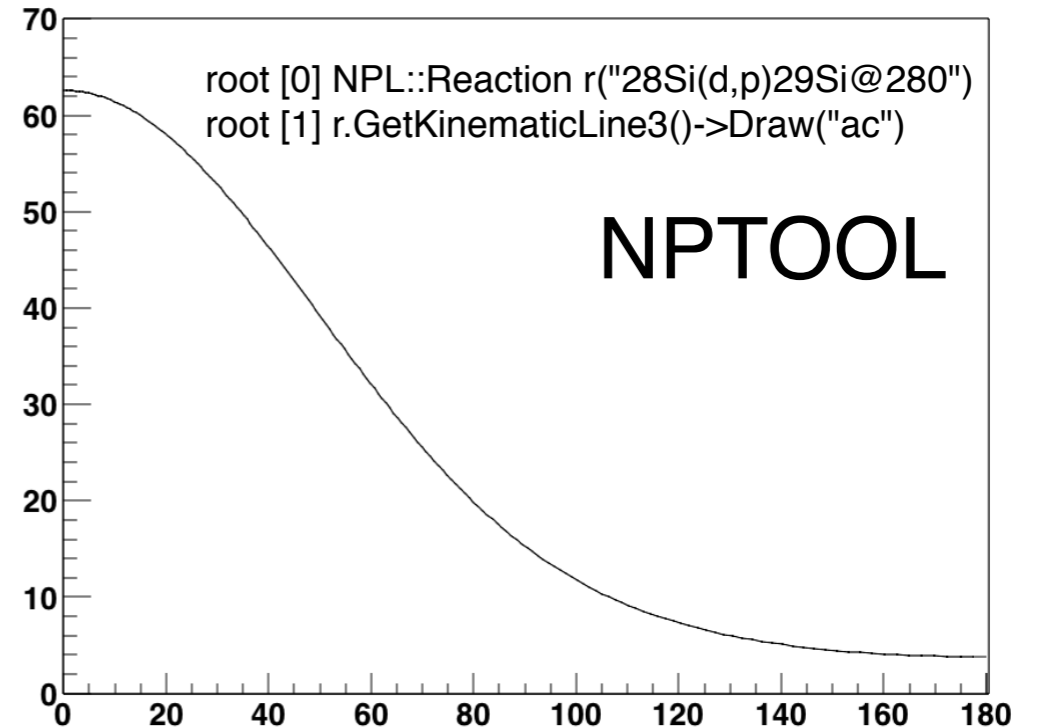
Reaction summary for  $^{28}\text{Si}+d \rightarrow p+^{29}\text{Si}$ ,  $E_k(^{28}\text{Si})=280$  MeV

- The maximum p energy is 62.577 MeV. The minimum p energy is 3.802 MeV.
- The maximum  $^{29}\text{Si}$  energy is 282.447 MeV. The minimum  $^{29}\text{Si}$  energy is 223.672 MeV. The maximum  $^{29}\text{Si}$  angle is 3.32 degrees.

$KE_3$  as a function of  $\theta_{cm}$ :



## Graph



Be careful with how different programs expect inputs to get consistent results!

# Some experimental considerations

- Production of Exotic Beams
- Intensity needs for Reaction Experiments
- Systematic uncertainties

# Units of beam intensities

Typical notation for intensity (or flux) of exotic beams:  
*particles per second, pps, 1/s, Hz, <sup>A</sup>X/s*

Primary beams are measured as electric current, A (C/s),  
typically *nA,  $\mu$ A, mA* (better to use ***enA, e $\mu$ A, emA***)

Often also “particle current”, expressed in “particle A”  
***pnA, p $\mu$ A*** (take out the beam charge state)

$$I_{particle} = \frac{I_{electric}}{charge\ state}$$

$$Intensity = \frac{I_{electric}}{beam\ charge} = \frac{I}{q \cdot e}, \left[ \frac{C/s}{C} = \frac{1}{s} \right] \quad \begin{array}{l} q: \text{beam charge state,} \\ e = \text{elementary charge} = 1.602 \cdot 10^{-19} \text{ C} \end{array}$$

→ Integrated current (total charge) gives total amount of incident particles



# Most common production reactions

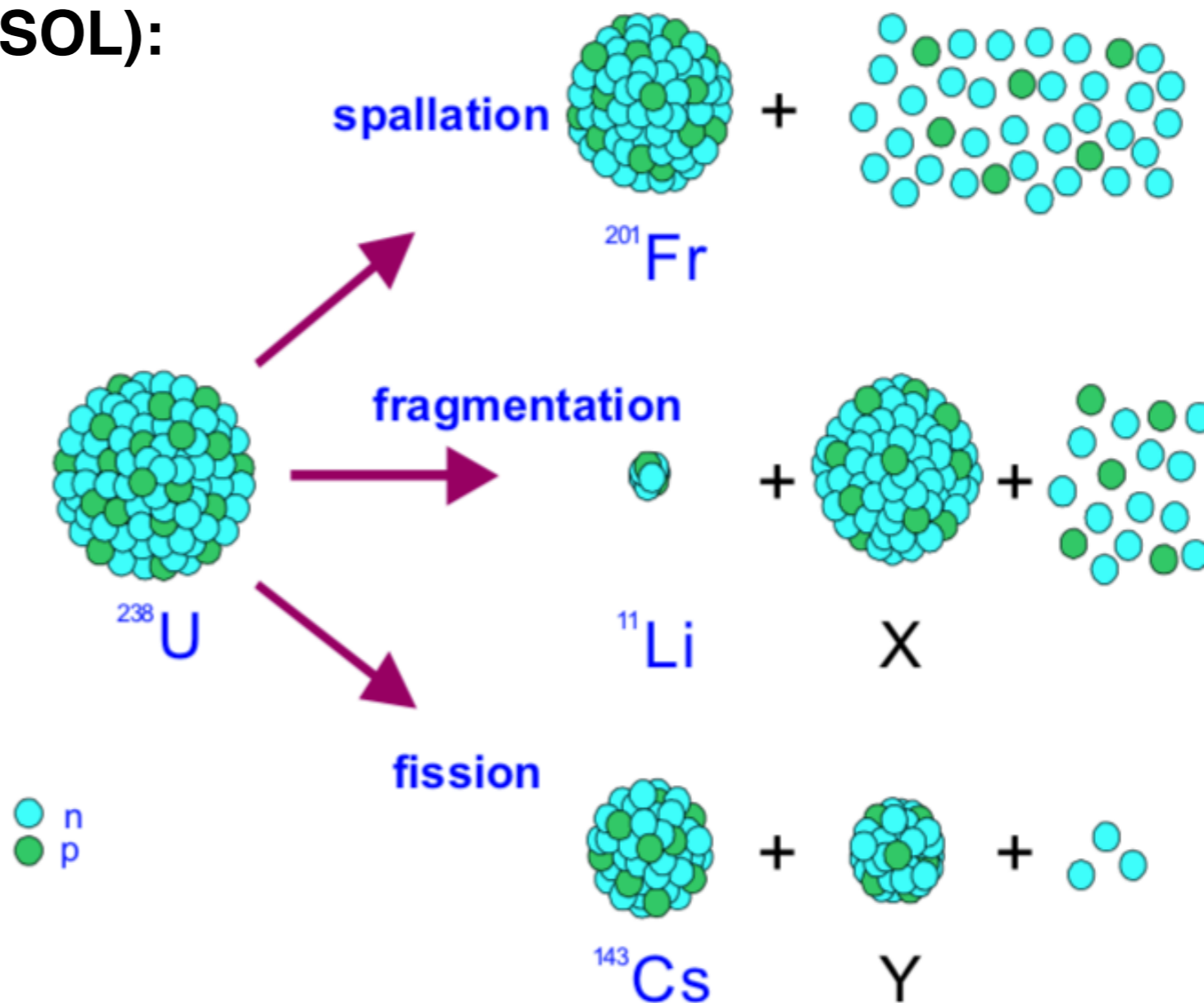
## Isotope Separation On-Line (ISOL):

High energy, high power  
p/e-/ $\gamma$  beam  
on heavy target

## In-flight:

High energy, high power  
heavy ion beam  
on typically a Be target

High energy:  $\sim 100$  MeV...1 GeV/u  
High power: up to MWatts!  
(1 MeV \* 1  $\mu$ A = 1W)

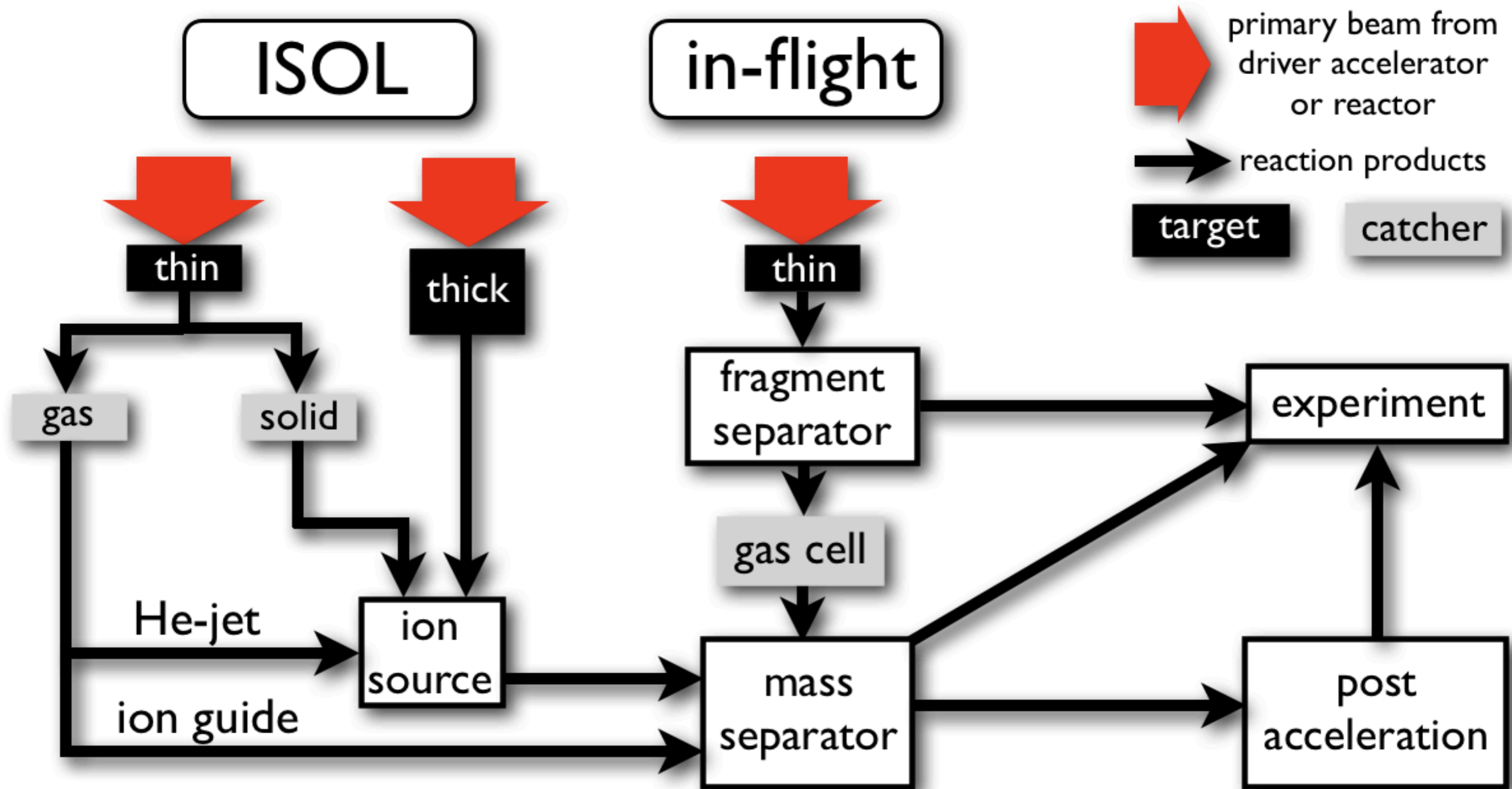


## At lower energies (both ISOL and in-flight):

Fusion evaporation, few nucleon transfer, deep-inelastic / multi-nucleon transfer



# Production of Exotic Beams



# Main features of ISOL and in-flight

## Isotope Separation On-Line:

- *thick target, thin target+ solid catcher* → slow release of products (up to seconds), chemically selective, need to ionize products
- *thin target or source + gas catcher* → faster  $\propto 0.1 \dots 10$  ms, products extracted typically as 1+ ion/molecule, chemically nonselective, but less efficient than thick catcher
- mass separator, charge state booster before reacceleration
  - typically beam with little to none impurities
- most common post-accelerator is tandem / linac
  - present facilities have availability of few MeV/u, soon up to  $\sim 10$  MeV/u
  - good quality beam after post-acceleration

## In-flight:

- products emerge from target with similar energy as the primary beam (up to GeV/u)
  - fast, depends on separator/spectrometer flight time, typical few  $\mu$ s
- chemically nonselective (can produce whatever reaction allows)
- efficient (products very forward focused towards the separator)
- secondary beam has typically considerable amount of impurities, energy/momentum spread, emittance
- tradeoffs between secondary beam energy, intensity, quality (can't have it all!)
  - for better beam quality need gas catcher, charge state booster, post-accelerator: energies available few MeV/u, soon up to  $\sim 10$  MeV/u

# Exotic Beam Intensity

Intensity of an Exotic Beam delivered to an experiment:

$$I = \sigma \cdot F \cdot N \cdot \epsilon_1 \cdot \epsilon_2 \cdot \epsilon_3 \cdot \epsilon_4 \cdot \epsilon_5 \cdot \epsilon_6 \cdot \epsilon_7 \quad [1/\text{s}, \text{pps}]$$

$\sigma$  : production cross section [ $\text{cm}^2$ ]

$F$  : primary-beam intensity [1/s]

$N$ : number production target nuclei [ $1/\text{cm}^2$ ]

$\epsilon_1$ : product release and transfer efficiency

$\epsilon_2$ : ion-source efficiency

$\epsilon_3$ : efficiency due to radioactive decay losses

$\epsilon_4$ : fragment separator efficiency

$\epsilon_5$ : gas cell efficiency

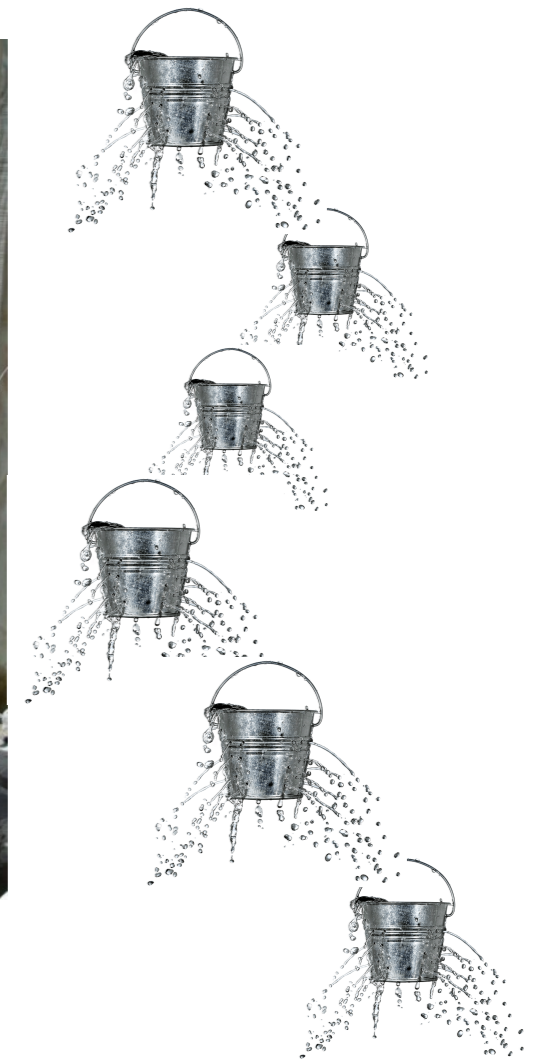
$\epsilon_6$ : mass separator efficiency

$\epsilon_7$ : post-acceleration efficiency

ISOL production part:  $\epsilon_1$ - $\epsilon_3$

Fragment separator:  $\epsilon_4$

Reaccelerated beams:  $\epsilon_5$ - $\epsilon_7$



# Exotic beam intensity requirement for an experiment?

How many counts per angle and how many incident energies are needed?

$$\left(\frac{d\sigma}{d\Omega}\right)_{exp} = \frac{N_{Detected}(\theta, \phi)}{N_{Beam} \cdot N_{Target} \cdot \epsilon \cdot d\Omega}$$

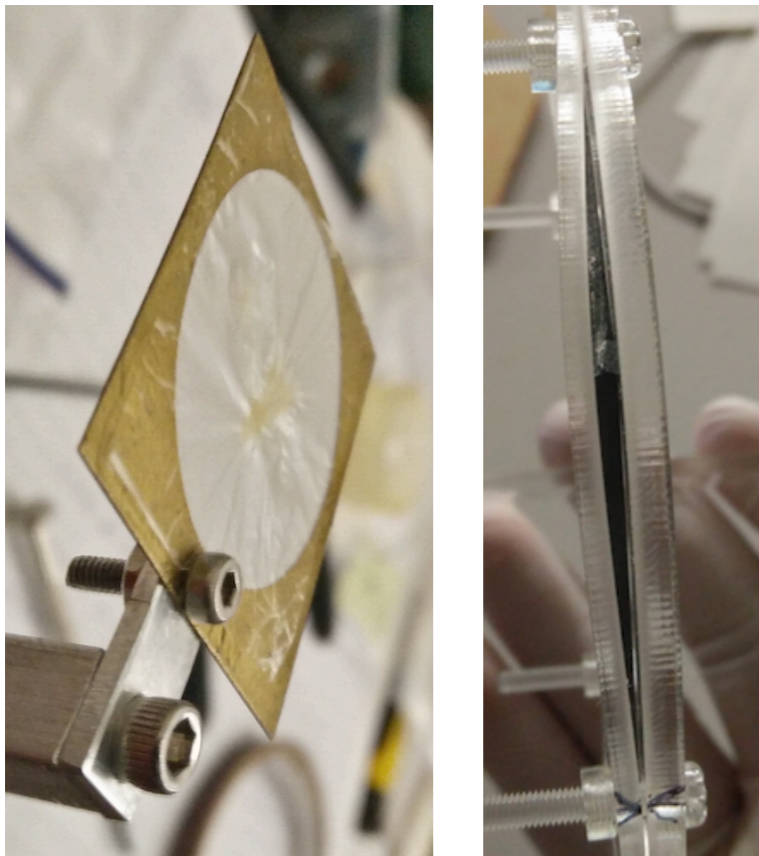
$$N_{beam} = \int_{beamtime} I dt; \quad I = \sigma \cdot F \cdot N \cdot \epsilon_1 \cdot \epsilon_2 \cdot \epsilon_3 \cdot \epsilon_4 \cdot \epsilon_5 \cdot \epsilon_6 \cdot \epsilon_7$$

$$N_{target} = \delta \cdot \frac{N_A}{M} = d \cdot \rho \cdot \frac{N_A}{M}$$

$\delta$ : mass/unit area [g/cm<sup>2</sup>],  $d$ : thickness [cm],  
 $\rho$ : density [g/cm<sup>3</sup>],  $M$ : molar mass [g/mol],  
 $N_A$ : Avogadro's number [1/mol]

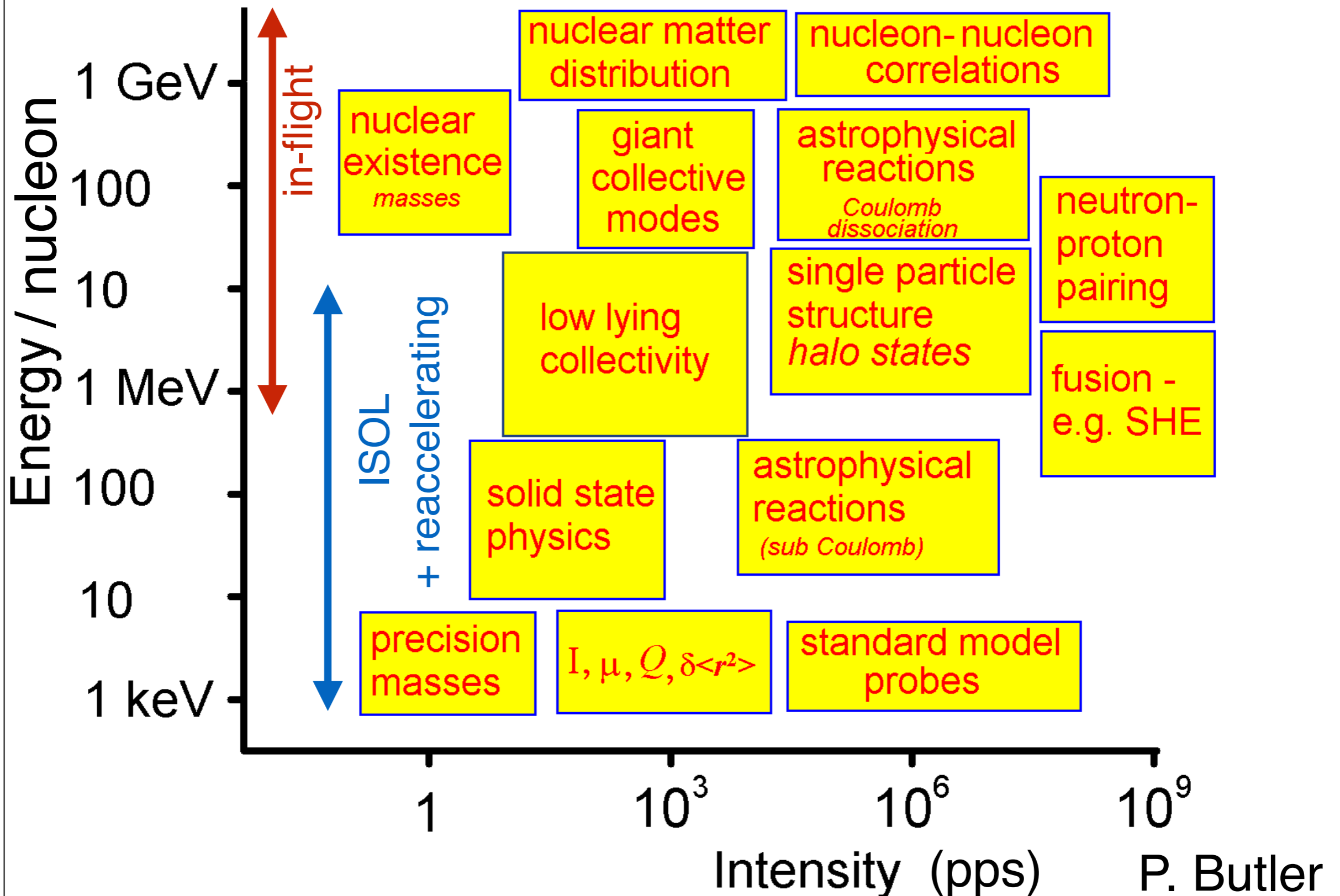
$\epsilon$ : detection efficiency — needs to be optimized  
 $d\Omega$ : solid angle — maximize coverage

How thick target can be used?

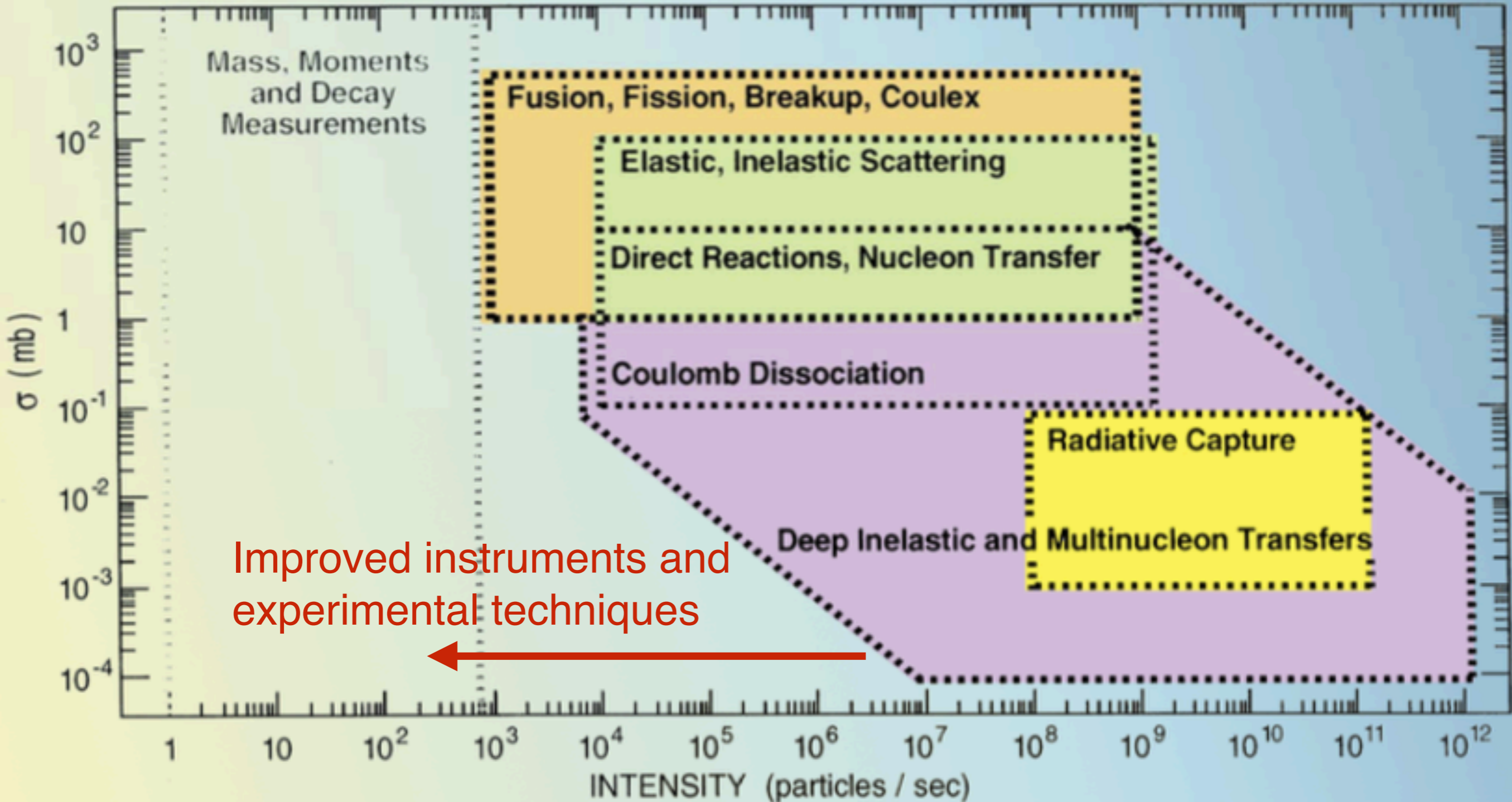




# Exotic Beam Physics Reach



# Intensity requirements for reaction experiments



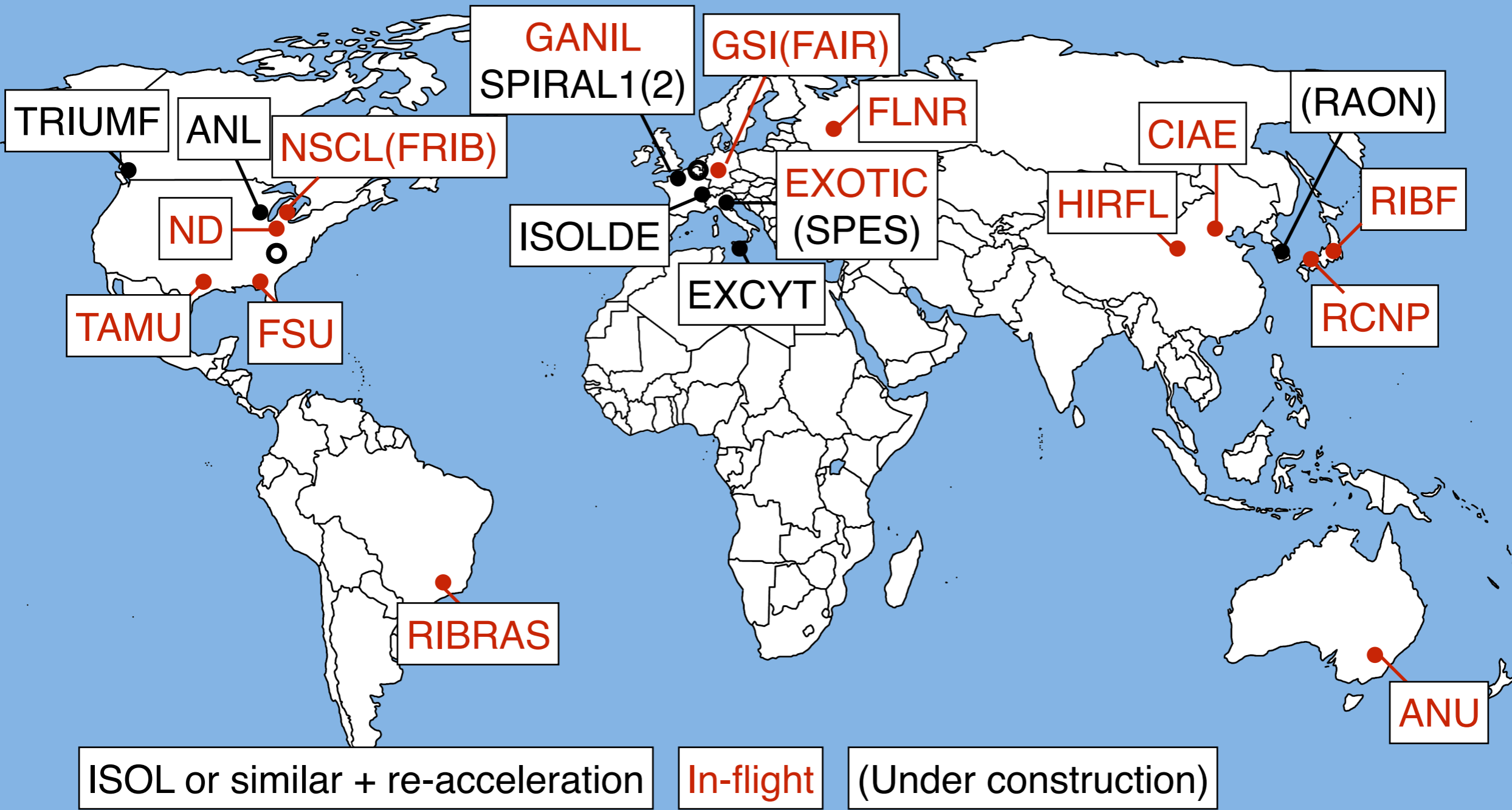
# Example: Requirements for transfers in inverse kinematics

K Wimmer 2018 *J. Phys. G: Nucl. Part. Phys.* **45** 033002

Type of experiment	$I$ (pps)	$d$ (mg cm <sup>-2</sup> )	$\sigma(E_{\text{exc}})$ (keV)
Fragmentation beams:			
Ejectile detection in spectrometer	$10^4$	20	700
Silicon detector array for recoil	$10^4$	10	600
Post-accelerated beams:			
Silicon detector array for recoil	$5 \times 10^4$	0.5	400
For high intensity beams	$10^6$	0.1	200
With $\gamma$ -ray detection	$10^5$	1.0	1
Magnetic spectrometer for recoil	$5 \times 10^4$	0.1	100
Active targets	$10^3$	10	100

# Where do you want to do your experiment?

## Facilities providing exotic beam for reactions



Note: Included only facilities with (radioactive/rare isotope/exotic) beams for reaction experiments. Some facilities may have more than one way to make beams! There are a lot of other existing facilities with stable beams or very low-energy (keV) exotic beams.



# Reaction Experiment Uncertainties

## **Statistical uncertainties:**

Mostly just how many counts one can get!

For Poisson statistics:  $\propto \sqrt{N}$

(assuming counting time separated independent events)

See e.g. IEEE Trans. Nucl. Sci. 43, 2501 (1996)

uncertainty of Gaussian peak centroid:

$$\text{var}(x_0) = \frac{\sigma^2}{A}$$

## **Systematic uncertainties:**

Beam related:

- Energy/momentum spread
- Angular spread
- Time spread

Beam characterization,  
tracking, ...

Target related:

- Target thickness, uniformity
- Target composition
- Target orientation

Target characterization,  
background measurements,  
alignment, ...

Detector related:

- Detector distance
- Detector orientation
- Detector efficiency

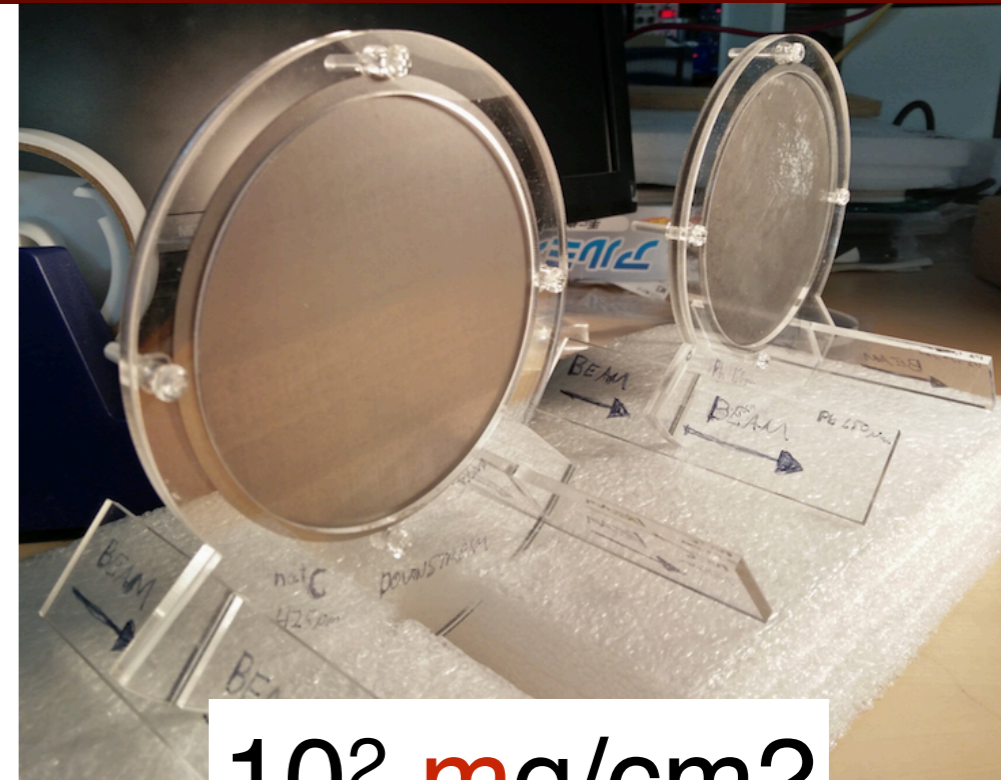
Understanding the instruments,  
simulations, alignment, ...

... and much much more, all specific for a given experiment!

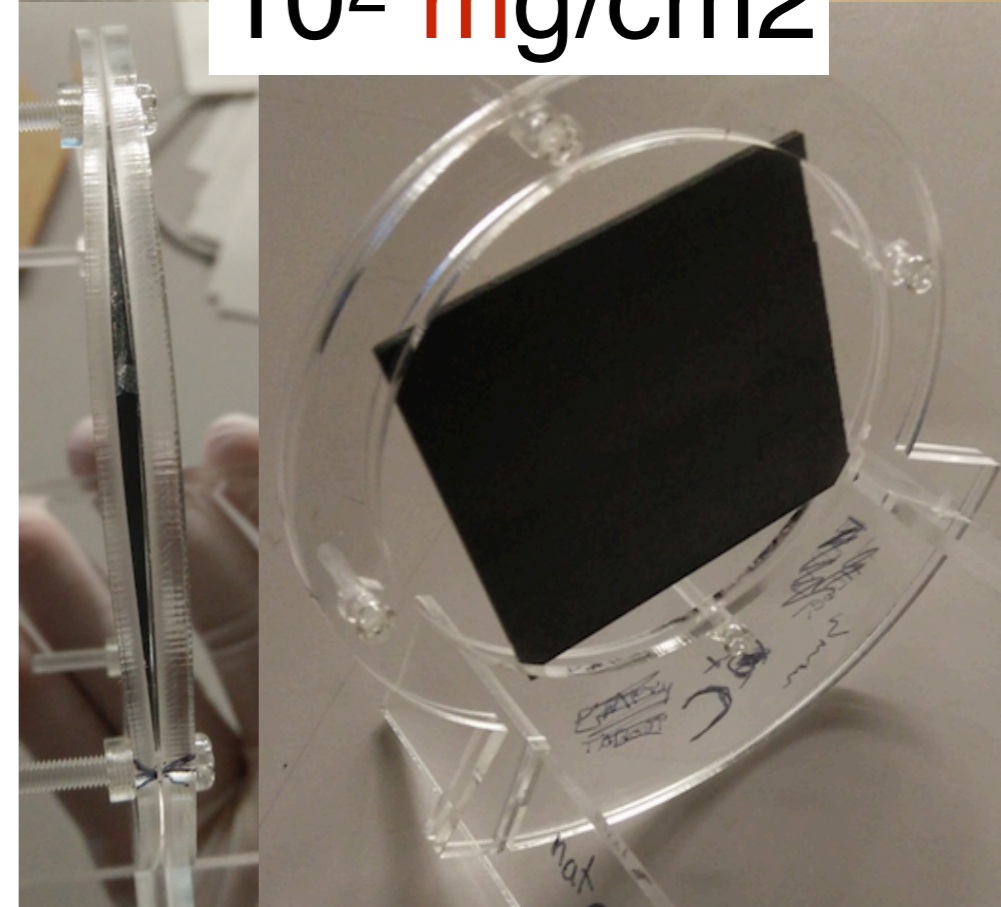
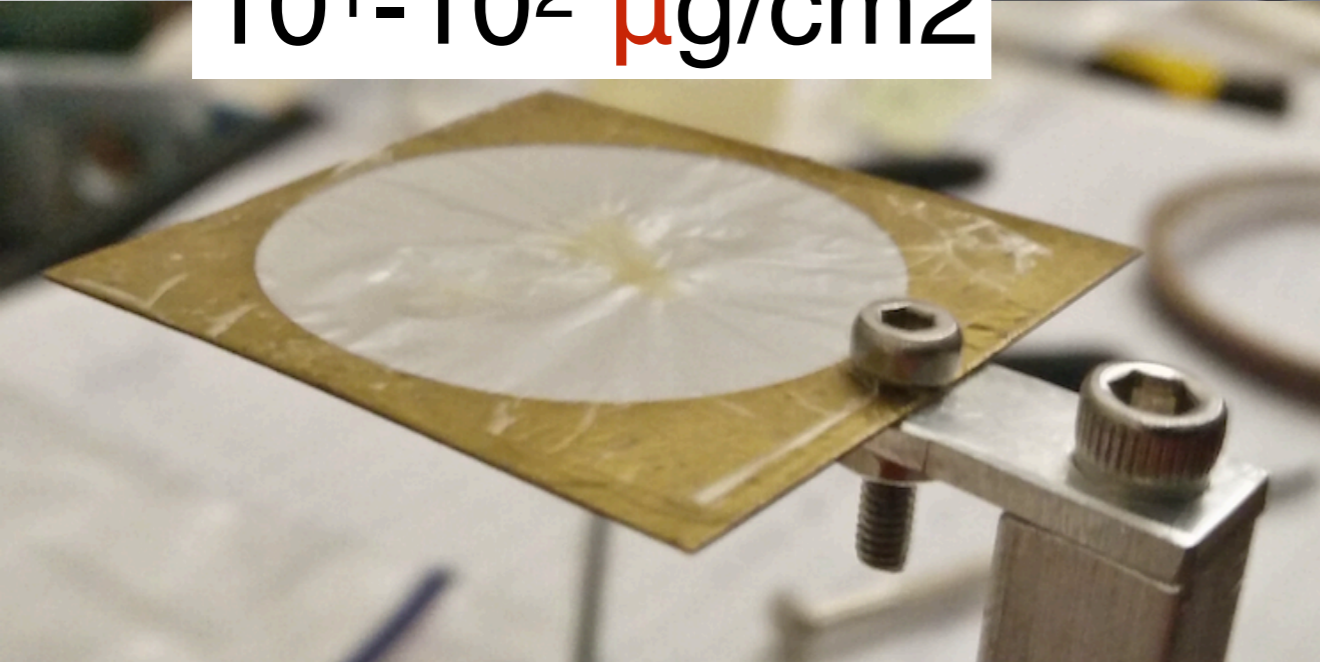
# Example: Target thickness / uniformity



$10^1 - 10^2 \mu\text{g}/\text{cm}^2$

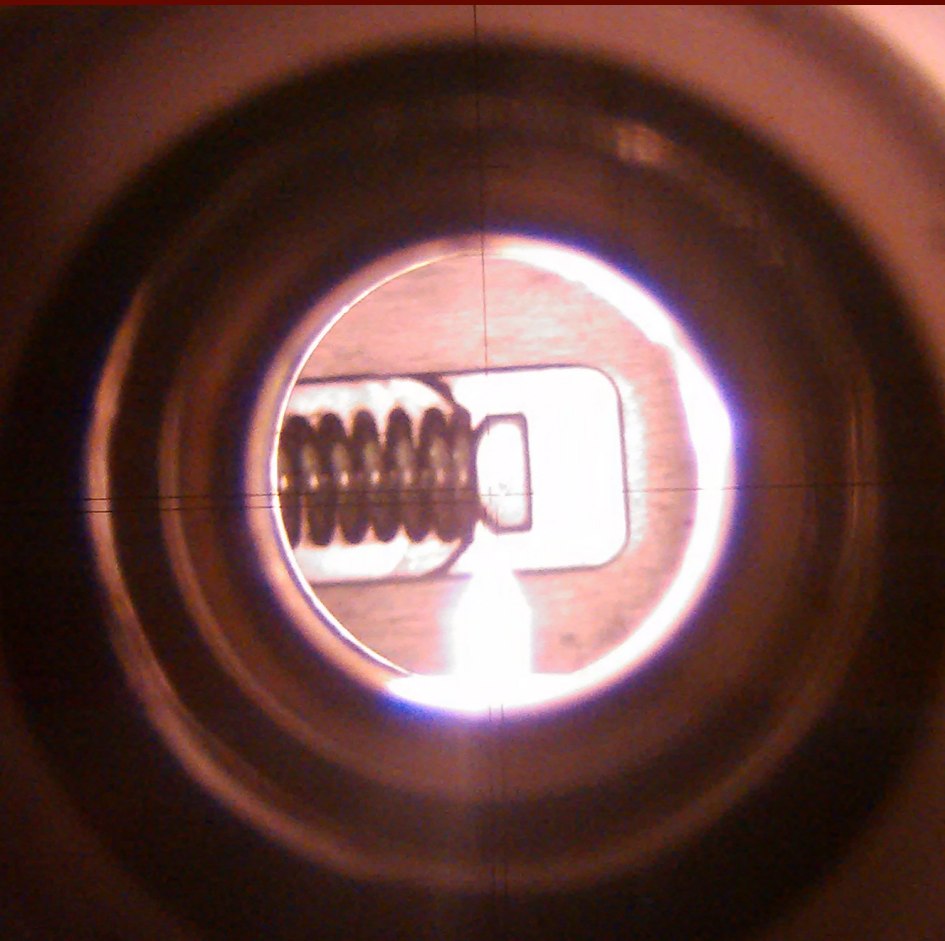


$10^2 \text{ mg}/\text{cm}^2$



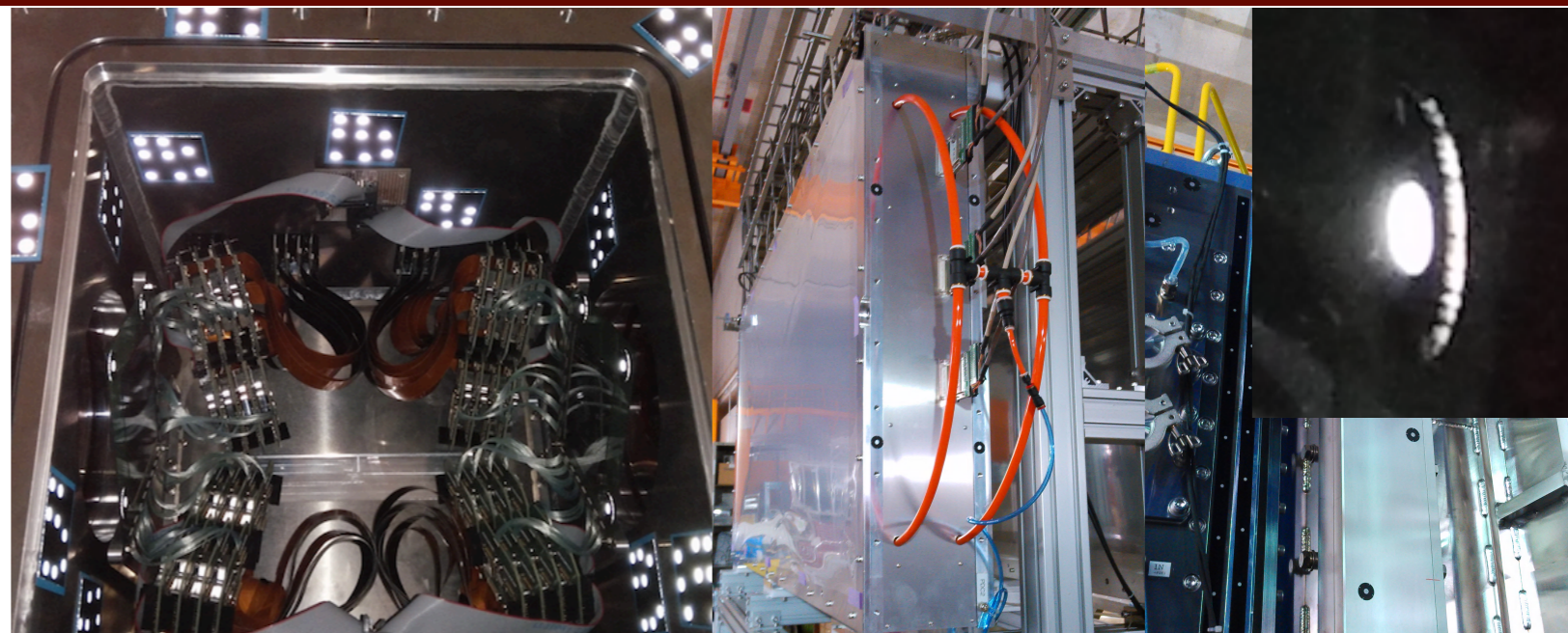


# Example: Setup alignment



Transit:  $< 0.1$  mm over  
few tens of m (on single axis)

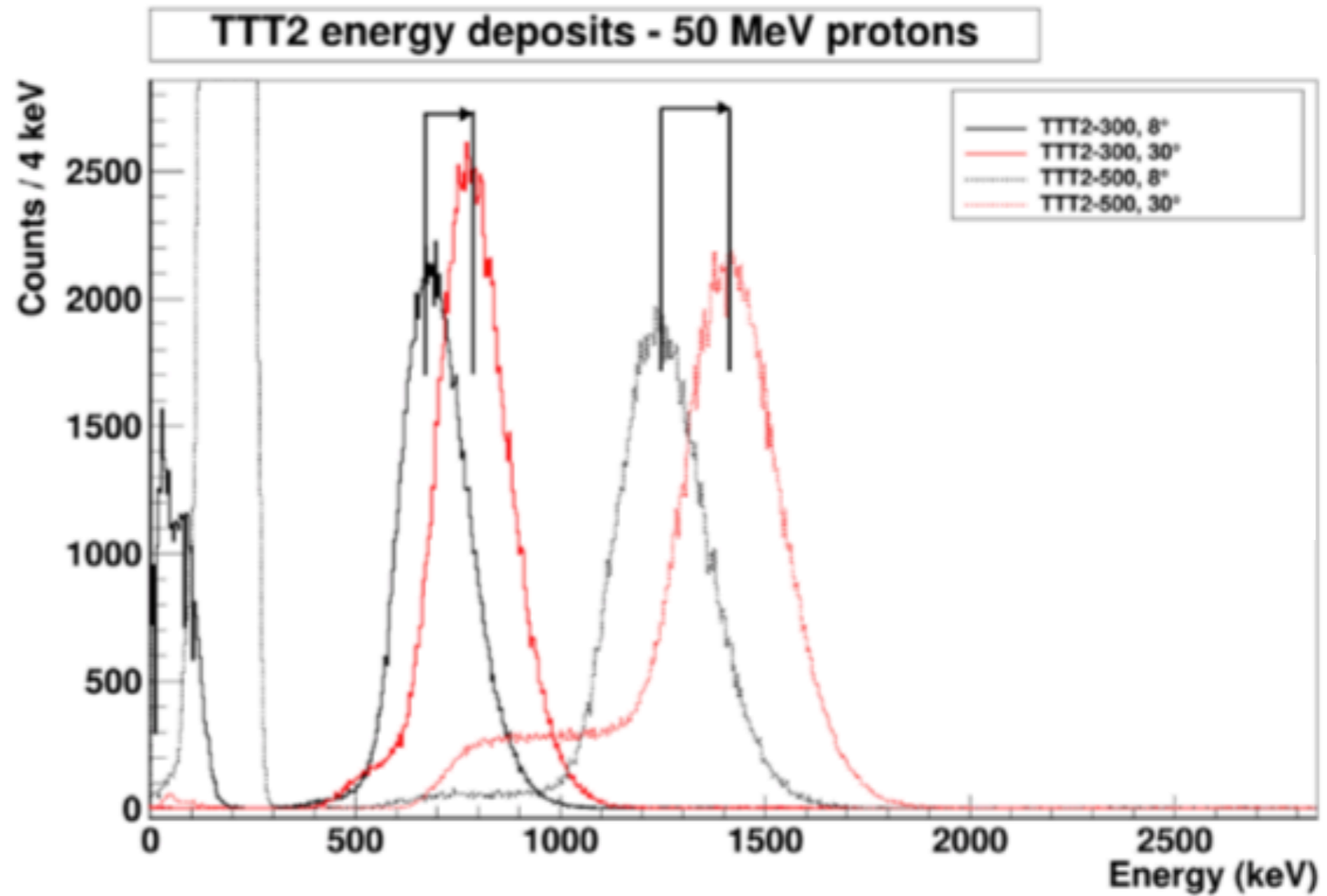
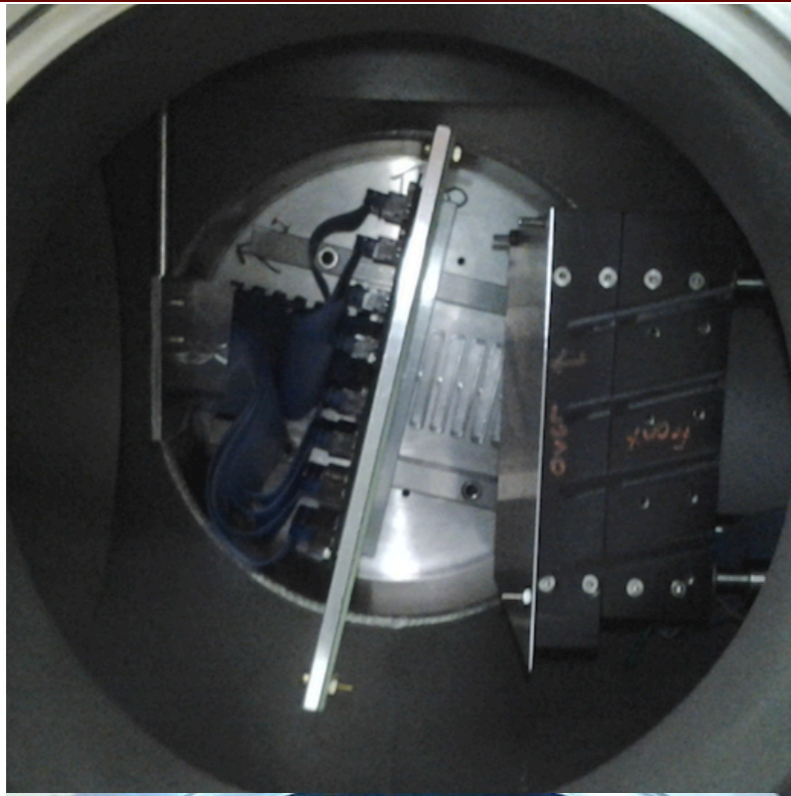
In not so distant future:  
Reconstruct setup in 3D  
with  $< 1$  mm precision  
from photos taken  
with an app?



Reconstruction from images with markers:  
 $< 1$  mm precision throughout experimental hall



# Example: Detector orientation



Know thy instruments!

# Summary lecture 1

- few basics of reaction experiments
- different reaction types
- production of exotic beams and intensity requirements for reaction experiments
- some experimental considerations

Lecture 2: Examples of reaction experiments with different approaches